Key-Update Mechanism for SDLSP

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Author list in alphabetical order, see https://www.ams.org/profession/leaders/culture/CultureStatement04.pdf. Andreas Hülsing, Tanja Lange, Fiona Weber (TU/e) Key-Update Mechanism for SDLSP

Authenticated Key Exchange

- SDLSP secures communication with symmetric keys.
- These can be replaced, but the update uses only symmetric cryptography.
 - Cannot recover from corruption!
 - The total number of keys grows quadratically with the number of parties.
 - The keys that a party has to know up-front grows linearly.
- Future mega-constellations may massively increase the number of communicating parties.

- Two parties, each with a long-term key-pair for authentication
- At least one party usually generates an ephemeral key-pair
 - Not used outside the exchange, secret-key disposed after exchange.
- The final output of an AKE is a shared secret that only the involved parties know.

Authenticated Key Exchange – In Our Use-Case

- Mission-Control and the Satellite both have a key-pair to authenticate themselves.
- They may have a previous shared secret. (The previous symmetric key)
- AKE computes a new shared secret that is secure even if the old one is leaked.
- Both parties can be certain of the identity of their peer.
- Can be run independently of a messaging-phase.

Advantages

- Total keys only scale *linearly* with the number of parties.
- Usable with a Public-Key-Infrastructure (PKI) No need to preload all keys.
- Possible to recover from corruption.

Confidentiality

Attacker does not learn information about resulting key.

- Forward-Secrecy: Even if he later corrupts a party.
- Post-Compromise-Secrecy: Even if he had corrupted the party before.
- Long-Term Security: Deal with "store-now, decrypt-later"-attacks.

Authenticity

Attacker cannot impersonate a different party.

- Prevent replay-attacks (common vulnerability).
- Good news: Attacks inherently have to be performed "live".

- Use two schemes in case one is broken
- Typically EC-schemes, e.g. Hashed Diffie-Hellman using X25519 and ECDSA.
- Can be done on protocol or primitive-level
 - primitive-level is generally simpler
 - it also results in an primitive-agnostic protocol \Rightarrow More options for implementers
- Fallback does not necessarily have to be pre-quantum!
- Combination trivial for Signatures.
- Less trivial for KEMs, but Hashing shared secrets and ciphertexts works.

- \bullet Long-term keys may also get corrupted \rightarrow should be updatable as well.
- Our protocol contains a mechanism for that.

Possible Approaches

$\mathsf{Signatures} + \mathsf{KEM}$



Figure 1: Signatures+KEM: The traditional Way.

- Requires replay-protection! (ctr)
- 1 Roundtrip
- Key-confirmation sensible, but not required.
- long-term-key-updates required if signature-scheme is stateful.
- Stateful scheme would enable few- and one-time signatures.

Triple-KEM and Dual-KEM



- Usually more efficient (KEMs instead of signatures).
- Essentially invulnerable to replay-attacks.
- Option to mix KEMs.
- Dropping {ct, pk, sk}_{resp} gives
 Dual-KEM, which does not authenticate the receiver.

Figure 2: Triple-KEM: The more modern way.

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- Obvious Choice: Kyber
- Ten times larger: Frodo
- Worth a look for special use-cases: Classic McEliece
- Not Size-Competitive with Kyber: BIKE and HQC
- Similar to Kyber, but lost PQC: Saber, NTRU, NTRU prime
- Broken: SIKE

Our Recommendations

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Our primary recommendation for general use is:

• Triple-KEM, using Kyber (and X25519) for all three KEMs

If satellite-authenticity is a given and the bandwidth-savings are important:

• Dual-KEM, using Kyber (and X25519) for both KEMs

Triple-KEM with Kyber



Figure 3: Triple-KEM

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We analyzed the protocol in a custom eCK-NEC model (= eCK, No Ephemeral Corruption)

- Simplified version of established eCK-model
- Assumes ephemeral randomness cannot be corrupted.
- Provides strong Confidentiality and Authenticity guarantees.

Security is usually defined via a "Game" in which an adversary tries to reach a winning-condition.

- n_i initiators and n_r responders run up to n_{s_i}/n_{s_r} initiator/responder-sessions each
- Adversary controls parties actions and the network
- Adversary can corrupt long-term keys and session-keys
- Winning conditions forbid trivial attacks
- Adversary wins
 - if he is able to distinguish an honestly generated key from randomness, or
 - if he is able to impersonate a party without corrupting its long-term-key.

Proven for Triple-KEM in eCK-NEC-model under reasonable assumptions:

- Honestly generated keys are indistinguishable from randomness. (Confidentiality)
- A party cannot be impersonated, as long as its long-term public key remains uncorrupted. (Authenticity)

Conjectured:

- Honestly generated keys remain confidential if the pre-shared key remains uncorrupted.
- Honestly generated keys remain confidential as long as one party's long-term key and the peer's ephemeral randomness remain uncorrupted.
- As long as a connection remains confidential (see above), no passive attacker can learn more about a new long-term public-key than can be extracted from ciphertexts for that public key. (Identity Hiding)

The same holds for **Dual-KEM**, *if* responder-authenticity is guaranteed out-of-band.

Formal Security Triple-KEM

There is no adversary that can win the eCK-NEC-game against Triple-KEM, with:

$$\mathsf{v}_{\mathcal{A},\,\mathsf{3KEM}}^{\mathsf{eCK-NEC}}\left(1^{\lambda}\right) \leq \begin{pmatrix} 3 & \cdot & \mathsf{Adv}_{\mathcal{A}_{1},\,\mathsf{H}}^{\mathsf{coll-res}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{s_{i}} & \cdot & \mathsf{EKEM}.\delta \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 3 & \cdot & \mathsf{Adv}_{\mathcal{A},\,\mathsf{EKEM}}^{\mathsf{IND-CCA}}\left(1^{\lambda}\right) \\ + & n_{s_{r}} \cdot n_{i} \cdot n_{r} \cdot \frac{1}{1-\mathsf{IKEM}.\delta} & \cdot & \mathsf{Adv}_{\mathcal{A}_{4},\,\mathsf{IKEM}}^{\mathsf{IND-CCA}}\left(1^{\lambda}\right) \\ + & n_{s_{i}} \cdot n_{i} \cdot n_{r} \cdot \frac{1}{1-\mathsf{RKEM}.\delta} & \cdot & \mathsf{Adv}_{\mathcal{A}_{4},\,\mathsf{RKEM}}^{\mathsf{IND-CCA}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 3 & \cdot & \mathsf{Adv}_{\mathcal{A}_{4},\,\mathsf{RKEM}}^{\mathsf{PRHO}}\left(1^{\lambda}\right) \\ + & (n_{s_{i}} + n_{s_{r}}) \cdot n_{i} \cdot n_{r} & \cdot & \mathsf{Adv}_{\mathcal{A}_{6},\,\mathsf{AEAD}}^{\mathsf{EUF-CMA}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 2 & \cdot & \mathsf{Adv}_{\mathcal{A},\,\mathsf{KDF}}^{\mathsf{PRF}}\left(1^{\lambda}\right) \end{pmatrix}$$

Ad

Formal Security Dual-KEM

There is no adversary that can win the eCK-NEC-game against Dual-KEM, with:

$$\mathsf{Adv}_{\mathcal{A},2\mathsf{KEM}}^{\mathsf{eCK-NEC}}\left(1^{\lambda}\right) \leq \begin{pmatrix} 2 & \cdot & \mathsf{Adv}_{\mathcal{A}_{1},\mathsf{H}}^{\mathsf{coll-res}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{i}} & \cdot & \mathsf{EKEM}.\delta \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 3 & \cdot & \mathsf{Adv}_{\mathcal{A},\mathsf{EKEM}}^{\mathsf{IND-CCA}}\left(1^{\lambda}\right) \\ + & n_{s_{r}} \cdot n_{i} \cdot n_{r} \cdot \frac{1}{1-\mathsf{IKEM}.\delta} & \cdot & \mathsf{Adv}_{\mathcal{A}_{4},\mathsf{IKEM}}^{\mathsf{IND-CCA}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 2 & \cdot & \mathsf{Adv}_{\mathcal{A},\mathsf{NHO}}^{\mathsf{PRHO}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 2 & \cdot & \mathsf{Adv}_{\mathcal{A},\mathsf{RAED}}^{\mathsf{PRF}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 2 & \cdot & \mathsf{Adv}_{\mathcal{A},\mathsf{RAED}}^{\mathsf{PRF}}\left(1^{\lambda}\right) \\ + & n_{i} \cdot n_{s_{i}} \cdot n_{r} \cdot n_{s_{r}} \cdot 2 & \cdot & \mathsf{Adv}_{\mathcal{A},\mathsf{RDF}}^{\mathsf{PRF}}\left(1^{\lambda}\right) \\ + & \mathsf{Adv}_{\mathcal{A},\mathsf{2KEM}}^{\mathsf{eCK-NEC}_{\mathsf{Case A}}}\left(1^{\lambda}\right) \end{pmatrix}$$

Where $\operatorname{Adv}_{\mathcal{A}, 2\text{KEM}}^{\text{eCK-NEC}_{\text{Case A}}}(1^{\lambda})$ Refers to the maximum achievable advantage for the adversary to cause an unpeered, complete initiator-session.

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Key-Update Mechanism for SDLSP

- We worked under the assumption that there are only very few initiators, because there are not many mission-control-centers.
 - Analysis deals with **all** users of a protocol, if this protocol is used widely that has to include everyone who controls a Satellite.
- Our model does not consider the possibility to corrupt ephemeral randomness.
 - In our experience most practitioners tend to believe that the solution to broken RNGs are not mitigations on the protocol-level, but rather fixing them on the system-level.

- Enable asymmetric key-updates for better scaling and security.
- Use post-quantum-secure algorithms for long-term security.
- Use an Authenticated Key Exchange (AKE) as Key-Update Mechanism
- Our Recommendation: Triple-KEM with Kyber+X25519
- Proposal builds on Post-Quantum Noise
- Formal Security-analysis in a simpler version of a standard model.

Appendix

KEMs – Sizes and Failure-rates

Scheme	SK	PK	СТ	δ
X25519	32	32	32	0
Kyber-512	1632	800	768	2^{-139}
Kyber-768	2400	1184	1088	2^{-164}
Kyber-1024	3168	1568	1568	2^{-174}
mceliece348864	6492	261120	96	0
mceliece460896	13608	524160	156	0
mceliece6688128	13932	1044992	208	0
mceliece6960119	13948	1047319	194	0
mceliece8192128	14120	1357824	208	0
FrodoKEM-640	19888	9616	9720	$2^{-138.7}$
FrodoKEM-976	31296	15632	15744	$2^{-199.6}$
FrodoKEM-1344	43088	21520	21632	$2^{-252.5}$

Signatures – Sizes

Scheme	SK	PK	Sig
Dilithium2	2544	1312	2420
Dilithium3	4016	1952	3293
Dilithium5	4880	2592	4595
Falcon-512	1281	897	666
Falcon-1024	2305	1793	1280
ECDSA	32	32	64

Triple-KEM – Packet Sizes

Scheme	Packet 1	Packet 2	Packet 3
	1664	1616	16
TKU(Kyber512+X25519)	2496	2464	16
TK(Kyber768+X25519)	2368	2256	16
TKU(Kyber768+X25519)	3584	3488	16
TK(Kyber1024+X25519)	3232	3216	16
TKU(Kyber1024+X25519)	4832	4832	16

Sign + KEM – Packet Sizes

Scheme	Packet 1	Packet 2	Packet 3
SK(Kyber512+X25519+Dilithium+ECDSA)	3348	3300	16
SKU(Kyber512+X25519+Dilithium+ECDSA)	4692	4644	16
SK(Kyber512+X25519+Falcon+ECDSA)	1594	1546	16
SKU(Kyber512+X25519+Falcon+ECDSA)	2523	2475	16
SK(Kyber512+X25519+XMSS-SHA2_10_256)	3364	3316	16
SKU(Kyber512+X25519+XMSS-SHA2_10_256)	3428	3380	16
SC(Kyber512+X25519,WOTS+(32,16))	3024	2992	16
SC(Kyber768+X25519,WOTS+(32,16))	2408	3312	16
SC(Kyber1024+X25519,WOTS+(32,16))	3792	3792	16
SC(Kyber1024+X25519,WOTS+(64,16))	10032	10032	16

Old Slides

- The traditional way of doing things.
- -> psk, ctr, e, s'[opt1], sig <- ekem, s'[opt2], sig
 - Requires replay-protection! (ctr)
 - 1 Roundtrip
 - Key-confirmation sensible, but not required.
 - long-term-key-updates required if signature-scheme is stateful.

- Use One-Time Signatures and always update the long-term key.
- No case-distinction.
- strong Post-Compromise-Authenticity!

```
-> psk, e, s', sig
<- ekem, s', sig
```

The modern way of doing things.

```
-> psk, skem, e, s' [opt1]
```

```
<- ekem, skem, s'[opt2]
```

```
-> confirm
```

- Usually more efficient (KEMs instead of signatures).
- Essentially invulnerable to replay-attacks.
- Option to mix KEMs.

- Obvious Choice: Kyber
- Ten times larger: Frodo
- Worth a look for special use-cases: Classic McEliece
- Not Size-Competitive with Kyber: BIKE and HQC
- Similar to Kyber, but lost PQC: Saber, NTRU, NTRU prime
- Broken: SIKE

Considered Signatures (1)

- Obvious Choice: Dilithium
- Serious Contender: Falcon

Scheme	SK	PK	Sig
Dilithium2	2544	1312	2420
Dilithium3	4016	1952	3293
Dilithium5	4880	2592	4595
Falcon-512	1281	897	666
Falcon-1024	2305	1793	1280
ECDSA	32	32	64

- Broken: Rainbow
- Weakened and lost PQC: GeMSS
- No clear advantage over SPHINCS+ (next slide) and lost PQC: Picnic

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- \bullet SPHINCS+ is essentially unusable here
- XMSS and LMS may be worth a thought
 - stateful signature-schemes
- WOTS too.
 - one-time signature scheme.

Table 6: SK = Sign + KEM, SC = Signature-Chain, TK = Triple-KEM

Scheme	Packet 1	Packet 2
SK(Kyber512+X25519+Dilithium+ECDSA)	4692	4644
SK(Kyber512+X25519+Falcon+ECDSA)	2523	2475
SK(Kyber512+X25519+XMSS-SHA2_10_256)	3428	3380
SC(Kyber512+X25519,WOTS+(32,16))	3024	2992
TK(Kyber512+X25519)	2496	2464

- All primitives can be changed to provide whatever security-level is desirable for them.
- Unless the reason for higher security-levels are brute-force attacks, different levels possibly quite reasonable.
- \Rightarrow Generally Level 1, sometimes Level 3

- HMAC widely used as dual-PRF/split-PRF.
- Secure, but useless if hashfunction is a Random Oracle.
- Several used primitives assume that it is.
- Not proven to be secure otherwise.
- No known practical attacks.

- Noise encrypts long-term public keys and signatures
- \bullet Primary purpose: Identitiy hiding \rightarrow Irrelevant here
- Overhead is comparatively small, but not zero.
- No analysis for case without encryption.
 - Relevant proofs do not rely on the encryption though.

- \bullet AES-GCM uses a \leq 128 bit tag for authentication
- Technically limits authenticity to 128 bit, though likely irrelevant in practice.
- CCSDS recommends 256 bit keys, but 128 bit tags.

- State-Reuse can effectively leak the secret key.
- Keys have to be stored securly on the satelite in the first place.
- How much can the control-center be trusted to manage its keys well?
- Is that need for trust worth the gain?